



# VIDYA BHAWAN, BALIKA VIDYAPITH

Shakti Utthan Ashram, Lakhisarai-811311(Bihar)

(Affiliated to CBSE up to +2 Level)

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SUB.: MATHEMATICS

## Square number:

If any natural number  $m$  can be expressed as  $n^2$ , where  $n$  is also a natural number, then  $m$  is known as a square number.

The square numbers are also called as perfect squares.

### Example:

Let  $m = 36$ .

Now, 36 can be expressed as  $6^2$ , where 6 is a natural number.

Therefore, 36 is a square number.

| Number | Square               | Number | Square               |
|--------|----------------------|--------|----------------------|
| 1      | $1 \times 1 = 1$     | 11     | $11 \times 11 = 121$ |
| 2      | $2 \times 2 = 4$     | 12     | $12 \times 12 = 144$ |
| 3      | $3 \times 3 = 9$     | 13     | $13 \times 13 = 169$ |
| 4      | $4 \times 4 = 16$    | 14     | $14 \times 14 = 196$ |
| 5      | $5 \times 5 = 25$    | 15     | $15 \times 15 = 225$ |
| 6      | $6 \times 6 = 36$    | 16     | $16 \times 16 = 256$ |
| 7      | $7 \times 7 = 49$    | 17     | $17 \times 17 = 289$ |
| 8      | $8 \times 8 = 64$    | 18     | $18 \times 18 = 324$ |
| 9      | $9 \times 9 = 81$    | 19     | $19 \times 19 = 361$ |
| 10     | $10 \times 10 = 100$ | 20     | $20 \times 20 = 400$ |

## Properties of Square Numbers:

1. The unit's place of square numbers can be 0, 1, 4, 5, 6 or 9.

No square number can end with 2, 3, 7 or 8.

2. If a number have 1 or 9 in its unit's place, then square of that number will end with 1.

### Example:

| Number | Square |
|--------|--------|
| 1      | 1      |
| 9      | 81     |
| 11     | 121    |

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**3. If a number have 4 or 6 in its unit's place, then square of that number will end with 6.**

**Example:**

| Number | Square |
|--------|--------|
| 4      | 16     |
| 16     | 36     |

**4. There will always be even number of zeros at end of any square number.**

**Example:**

| Number | Square |
|--------|--------|
| 10     | 100    |
| 20     | 400    |

**5. On combining two consecutive triangular numbers we get a square number.**

**Example:**

$1 + 3 = 4 = 2^2$        $3 + 6 = 9 = 3^2$        $6 + 10 = 16 = 4^2$

**6. There are  $2n$  non-perfect square numbers between the squares of the numbers  $n$  and  $(n+1)$ .**

**Example:**

Between  $3^2 = 9$  and  $4^2 = 16$ , there lies 6 numbers which are 10, 11, 12, 13, 14, and 15.

**7. If the number is a square number, then it has to be the sum of successive odd numbers starting from 1.**

**Example:**

For  $3^2 = 9$ , the sum of successive odd numbers from 1 will be  $1+3+5 = 9$ .

*Note:* If a natural number cannot be expressed as a sum of successive odd natural numbers starting with 1, then it is not a perfect square.

**8. Square number can be summation of two consecutive natural numbers.**

**Example:**

$5^2 = 25 = 12 + 13$ ;  $7^2 = 49 = 24 + 25$ , etc.

**9. Product of two consecutive even or odd natural numbers.**

**Example:**

$$11 \times 13 = (12-1) \times (12+1) = 12^2 - 1;$$

$$13 \times 15 = (14-1) \times (14+1) = 14^2 - 1$$

$$\text{So, in general } (a+1) \times (a-1) = a^2 - 1.$$